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SPECTROSCOPY AND THERMODYNAMICS

I.

MOMENTS OF INERTIA OF METHYL BROMIDE

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EQUILIBRIUM CONSTANTS OF THE REACTION CH₃Br + HCl 之 CH₃Cl + HBr MOMENTS OF INERTIA OF METHYL BROMIDE

 \mathbf{BY}

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I. MOMENTS OF INERTIA OF METHYL BROMIDE

I. Introduction.

In recent years, the application of quantum mechanics to chemical questions has proved especially fruitful in the treatment of problems which hitherto could only be dealt with correctly from a purely thermodynamical point of view, such as the determination of standard entropies, chemical affinities, etc. As quantum mechanics mainly work with symbols to be experimentally determined by means of spectroscopical methods, a near relationship between spectroscopy and thermodynamics has been established.

A survey of the work accomplished within this common field of spectroscopy and thermodynamics up to 1936 was given by $K_{ASSEL.^1}$ It is a striking fact that most of the compounds investigated are simple inorganic molecules, and the development of the last ten years has hardly altered the situation. This is due partly to the restrictions laid upon the experimentator when working with unstable organic molecules, partly, as will be pointed out later, to theoretical difficulties arising when the more complex organic molecules are treated.

In the present paper the author attempts to combine the determination of the heat capacity of CH_3Br , carried out by EGAN and KEMP,² with an analysis of the optical spectra of the same compound. In order to ascertain the correctness of the vibrational analysis, the Raman spectrum of CH_3Br was renvestigated. Our result is in conformity with the results obtained earlier. The vibration frequencies, therefore, can only be unessentially changed by future work. As will be shown in the present paper, the combination of thermodynamical and spectroscopical data leads to definite values of the moments of inertia of CH_3Br .

¹ Kassel, Chem. Rev. 18, 277 (1936). ² Egan and KEMP, J. Am. Chem. Soc. 60, 2097 (1938).

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II. Entropy in Terms of Spectroscopically Determinable Quantities.

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The fundamental equations were coherently published by $G_{IAUQUE.^1}$ The general expression for the absolute entropy of one mole of an *ideal gas*, S^o, is:

 $\mathrm{S}^{\circ} = \, \mathrm{S}^{\circ}_{\mathrm{trans}} + \mathrm{R} \, \Bigl(\mathrm{ln} \mathrm{Z} + \mathrm{T} \, \frac{\mathrm{d} \mathrm{ln} \mathrm{Z}}{\mathrm{d} \mathrm{T}} \Bigr). \label{eq:solution}$

Here, R is the gas constant, T the absolute temperature, and S_{trans}° the translational entropy.² Z is the so-called 'state sum'. For an ideal gas the individual molecule has a well-defined ground state, a first excited level, etc., unquantized translational energy being neglected. The separation of the translational energy from the quantized vibrational-rotational energy is correct for the ideal gas state because, in the field-free space, the part of the Schroe dinger equation dealing with the translational movement of the molecule, factors out.³ In Table I a survey of present circum stances is taken.

| Table | 1 | |
|-------|---|--|
|-------|---|--|

| State | Energy minus translational energy | A priori probality of state | Number of molecules in state |
|------------------|---|-----------------------------------|--|
| Ground State | ε' | Po | |
| 1. excited level | $\varepsilon_0' + \varepsilon_1$ | $\mathbf{p_1}$ | $Ap_1 e^{\overline{kT}} - \varepsilon_1$ |
| 2. excited level | $\varepsilon_0' + \varepsilon_2$ | $\mathbf{p_2}$ | Ap ₂ e ^{kT} |
| | | • | 81 bT |
| i. excited level | $\varepsilon'_0 + \varepsilon_i$. | р, | Ap _i e ^m |

If the total number of molecules is denoted by N, we obtain

$$N = A\left(p_0 + \sum_{i=1}^{\infty} p_i e^{\frac{-\epsilon_i}{kT}}\right) \hspace{1.5cm} Z = p_0 + \sum_{i=1}^{\infty} p_i e^{\frac{-\epsilon_i}{kT}} \hspace{1.5cm} .$$

¹ GIAUQUE, J. Am. Chem. Soc. 52, 4808 (1930).

² The subscript zero applies to the ideal state throughout this and the following paper.

³ KASSEL, Chem. Rev. 18, 279 (1936).

Within this field most rules are conveniently formulated by means of Z, as for example in (I). It should, however, be kept in

mind that the state sum is sometimes defined as $Z = \sum_{i=0}^{\infty} p_i e^{\frac{-(\varepsilon_i + \varepsilon'_0)}{kT}}$,

where ε_0 is zero. This is done e.g. in the important paper by Gordon and BARNES.¹ As is seen from the papers cited,

Z (Giauque) =
$$e^{\frac{\tilde{\epsilon}'_0}{kT}}$$
Z (Gordon and Barnes).

However, Giauque's definition seems to be more commonly used. For the ideal gas state

$$\mathbf{S}^{\circ}_{\mathrm{trans}} = \frac{3}{2} \mathrm{Rln}\mathbf{M} + \frac{5}{2} \mathrm{Rln}\mathbf{T} - \mathrm{Rln}\mathbf{P} + \frac{5}{2} \mathbf{R} + \mathbf{C} + \mathrm{Rln}\mathbf{R}'.$$

Here, M is the molecular weight proportional to oxygen, P the pressure in atmospheres, R' the gas constant in ccm atmospheres per degree and $C = Rln \cdot \frac{(2\pi k)^{3/2}}{h^3 N^{5/2}}$, where k is Boltzmann's constant, h Planck's constant and N is Avogadro's number. Thus, for one mole of an ideal gas

$$S^{\circ} = \frac{3}{2} \operatorname{Rln}M + \frac{5}{2} \operatorname{Rln}T - \operatorname{Rln}P + \frac{5}{2} \operatorname{R} + \operatorname{C} + \operatorname{Rln}R' + \\ + \operatorname{R}\left(\operatorname{ln}Z + \operatorname{T}\frac{\operatorname{dln}Z}{\operatorname{dT}}\right).$$
(II)

Let us now try to find the special form for (II) in the case of CH₃Br by following the approximations step by step.

As a first approximation let us assume that no molecules are in a state of electronic excitation. This is practically true for most molecules up to ca. 1500°, because the available kinetic energy per degree of freedom at 0° C is ~ 100 cm⁻¹ while the electronic excitation energy is 10000—100000 cm⁻¹.

Furthermore, in the case of CH_3Br , p_0 , the a priori probability of the electronic ground level, is 1. Hence

Gordon and BARNES, J. Chem. Phys. 1, 298 (1933).

$$Z = 1 + \sum_{i=1}^{\infty} p_i e^{\frac{-\epsilon_i}{kT}}$$

where ε now simply means the height of one of the vibrational rotational levels above the ground level. By defining $\varepsilon_0 = 0$ we may write:

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$$Z = \sum_{i=0}^{\infty} p_i e^{\frac{-\varepsilon_i}{kT}},$$

where p_0 is equal to 1.

Generally, the vibrational and rotational energies of a mole cule vary almost independently of each other. However, special interest will be paid to the case where they are completely independent. The correctness of this assumption will be discussed later. The assumption means that each ε_i can be written as ε_n (vib) + ε_j (rot), defining ε_0 (vib) = ε_0 (rot) = 0. To every fixed value of ε_n (vib) belongs the same series of rotational levels ε_0 (rot), ε_1 (rot), ε_2 (rot)..., superposed on the vibrational level. Simultaneously, p can be written as p_n (vib) p_j (rot), be cause of the independence of the a priori probabilities of the vibrational and the rotational states. As p_0 (vib) = p_0 (rot) = 1 we get:

$$Z = \sum_{i=0}^{\infty} p_i e^{\frac{-\varepsilon_i}{kT}} = \sum_{n=0}^{\infty} \sum_{j=0}^{\infty} p_n (vib) p_j (rot) e^{\frac{-\varepsilon_n (vib) - \varepsilon_j (rot)}{kT}}$$
$$= \sum_{n=0}^{\infty} p_n (vib) e^{\frac{-\varepsilon_n (vib)}{kT}} \sum_{j=0}^{\infty} p_j (rot) e^{\frac{-\varepsilon_j (rot)}{kT}} = Z_{vib} \cdot Z_{rot}.$$

The entropy expression (I), therefore, is changed into

 $\mathrm{S}^\circ = \mathrm{S}^\circ_{\mathrm{trans}} + \mathrm{S}^\circ_{\mathrm{vib}} + \mathrm{S}^\circ_{\mathrm{rot}}.$

a. Calculation of the vibrational entropy.

Here the simplifying assumption will be made that the molecules of the system perform harmonic vibrations. For a diatomic molecule, with only one vibration frequency, the vibrational energy diagram is considered to consist of a serie of equidistant levels instead of the actually occurring converging ones.



Fig. 1 is the energy diagram for a harmonic oscillator with one degree of freedom. $\varepsilon_i(\text{vib}) = i \cdot \varepsilon_1(\text{vib})$. The a priori probability of each level is 1. Therefore

Z(vib., diatomic molecule) = $\sum_{i=0}^{\infty} e^{\frac{-\varepsilon_i(vib)}{kT}} = \frac{1}{1 - e^{\frac{-\varepsilon_i(vib)}{kT}}}.$

If, moreover, we imagine a molecule with two vibrational degrees of freedom, an energy pattern like that shown in fig. 1 (but with a different distance between adjacent levels) must be superposed on each of the levels of fig. 1. Thus, when calculating $Z_{\rm vib}$, the situation is completely analogous to that described earlier, which permitted the rotational state sum $Z_{\rm rot}$ to be factored out from the combined $Z_{\rm rot + vib}$: each vibrational level is superposed with the same series of other vibrational levels. Consequently, in the case of two vibrational degrees of freedom, $Z_{\rm vib}$ consists of two factors, each of the form stated for the diatomic molecule. Generally, for a molecule with n atoms, possessing 3n-6 fundamental frequencies $v_{\rm f}$, where $hv_{\rm f} = \varepsilon_{\rm f}$, we get:

$$Z_{\text{vib}} = \prod_{1}^{3n-6} \frac{1}{1-e^{\frac{-\epsilon_{r}}{\overline{kT}}}}$$
(1)

If v_f is a double degenerate frequency, e.g. $v_f = v_{f+1}$, the ame factor appears twice in (1); if v_f is threefold degenerate, the same factor appears three times, etc.

is mostly very good. The ground level and the first excited level appear with their correct energy values in (1), the second and higher excited levels appear with an energy value which is some what $(1-2^{\circ})_{0}$ too high. But, as the second excited level general lies higher than 500 cm⁻¹ (in most cases much higher), the frace tion of molecules in this state is very small, viz. approximately -500

 $e^{100} \sim 0.006$ at room temperature. Consequently, we may write

$$S_{vib}^{\circ} = R \sum_{f=1}^{f=3n-6} \left(\frac{\frac{\varepsilon_{f}}{kT}}{\frac{\varepsilon_{f}}{e^{\overline{kT}}-1}} - \ln\left(\frac{-\varepsilon_{f}}{1-e^{\overline{kT}}}\right) \right).$$

$$\frac{\frac{\epsilon_{f}}{kT}}{e^{\frac{\epsilon_{f}}{kT}}-\ln\left(1-e^{-\frac{\epsilon_{f}}{kT}}\right)} \text{ is often abbreviated as } S_{Ein}(\nu_{f},T).$$

We then obtain:

$$\mathbf{S}_{\text{vib}}^{\circ} = \mathbf{R} \sum_{\mathbf{f}=1}^{\mathbf{f}=3n-6} \mathbf{S}_{\text{Ein}}(v_{\mathbf{f}}, \mathbf{T}).$$

b. Calculation of the rotational entropy.

$$Z_{rot} = \sum_{j=0}^{\infty} p_j(rot) e^{\frac{-\varepsilon_j(rot)}{kT}}$$

A common expression valid for all types of molecules; et at room temperature, cannot be given. For small molecules direct summation generally pays (H2, HF). For larger molecule such as CH₃Br, approximate formulas have been developed CH_aBr has two different principal moments of inertia, A and If C be the moment of inertia around the C-Br axis,

$$\varepsilon_{j}(\text{rot}) = \frac{h^{2}}{8\pi^{2}A} \left[k \left(k+1 \right) + n^{2} \left(\frac{A}{C} - 1 \right) \right] \qquad |n| \leq k.$$

The approximation made by assuming harmonic vibration k and n are the integral quantum numbers. For a state with quantum numbers n, k the a priori weight is 2 k + 1. The summation to be made according to (2) is considerably more complicated than the summation of Z_{vib}. Asymptotically the sum can be expressed by

$$Z = \pi^{\frac{1}{2}} \delta^{-\frac{3}{2}} e^{\beta_{4}} (\beta + 1)^{-\frac{1}{2}} \left[1 + \frac{\beta}{12} (\beta + 1)^{-1} \delta \cdots \right],$$

ere $\delta = \frac{h^{2}}{8 \pi^{2} A k T}$ and $\beta = \frac{A}{C} - 1.^{1}$

In the case of CH₃Br the expression in the square brackets in good approximation is equal to 1. As A ~ 10^{-38} gcm² we get $\delta \sim \frac{40 \cdot 10^{-54}}{8 \cdot 10 \cdot 10^{-38} \cdot 1.4 \cdot 10^{-16} \cdot T} \sim \frac{1}{2.8 \text{ T}}$. A/C ~ 15. Thus $\beta \sim 14$ and $\frac{\beta}{12}(\beta+1)^{-1}\delta \sim \frac{1}{40 \text{ T}}$. At 100° K this is less than 0.001 and can safely be neglected.

 $e^{\theta_{i}} \sim e^{\overline{11T}}$. At 100° K this is approximately 0.001. Consequently, in good approximation we have

$$Z_{\rm rot} = \pi^{\frac{1}{2}} \delta^{-\frac{3}{2}} (\beta + 1)^{-\frac{1}{2}} \text{ and } S_{\rm rot}^{\circ} = \operatorname{Rln} \cdot \left[\frac{8\pi^{\frac{7}{3}} A^{\frac{3}{8}} C^{\frac{1}{8}} k \operatorname{Te}}{h^2} \right]^{\frac{3}{2}}.$$

Finally,

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wh

$$S^{\circ} = S^{\circ}_{\text{trans}} + S^{\circ}_{\text{vib}} + S^{\circ}_{\text{rot}} = R \left[\frac{3}{2} \ln M + \frac{5}{2} \ln T - \ln P + \frac{5}{2} + \frac{C}{R} + \ln R' + \sum_{f=1}^{3n-6} S_{\text{Ein}}(\nu_f, T) + \ln \left(\frac{8\pi^3 A^3 C^3 k T e}{h^2} \right)^{\frac{6}{2}} \right].$$

Looking more closely into the matter and taking into consideration the possible presence of spin isomers, optical isomers, and a possible multiplicity of the electronic ground state differing from unity, we find:

¹ KASSEL, loc. cit.

$$S^{\circ} = R \left[\frac{3}{2} \ln M + \frac{5}{2} \ln T - \ln P + \frac{5}{2} + \frac{C}{R} + \ln R' + \right]$$
$$+ \sum_{f=1}^{f=3n-6} S_{Ein}(v_{f}, T) + \ln \left(\frac{8 \pi^{\frac{2}{3}} A^{\frac{2}{3}} C^{\frac{1}{8}} K T e}{h^{2}} \right)^{\frac{3}{2}} \frac{P_{e} P_{n} I}{\sigma} \right].$$

(IV

Here, p_{e} is the a priori probability of the electronic ground state $(= 1 \text{ for } CH_3Br)$, p_n is the number of nuclear spin isomers, Iis the number of optical isomers (= 1 for CH₂Br), and σ is the 'symmetry number', equal to the number of permutations of identical atoms in a single molecule which could be carried out by rotating the molecule (= 3 for CH_3Br). The number p_n is unknown for the molecule in question, which means that the absolute entropy given by (IV) cannot be calculated. However, most entropy determinations are carried through at temperatures between a few degrees above the absolute zero and room tem perature. As in all cases the calorimetric effect of the presence of spin isomers is detectable only in the immediate neighbour hood of 0° K, this means that such effects are not included in the experimentally determined entropy values. These experimental values may, therefore, be put equal to S, calculated from (IV). putting $p_n = 1$.

In this connexion it is worth mentioning that in the calculation of equilibrium constants for chemical reactions above 100° K all nuclear spin effects can be ignored¹.

Defining $A' = A \cdot 10^{38}$ and $C' = C \cdot 10^{38}$, and using the usual numerical values for the natural constants, we get the formula

$$S^{\circ} = R \left[2.307 + 4 \ln T + \frac{3}{2} \ln M + 1/2 \ln A'^{2} C' + \right. \\ \left. + \ln \frac{p_{e} n_{n} I}{\sigma} + \sum_{f=1}^{f=3n-6} S_{Ein}(\nu_{f}, T) \right],$$

valid for the entropy of one mole in the ideal gas state at pressure of one atmosphere.

¹ GIBSON and HEITLER, Z. Phys. 49, 465 (1928).

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III. Moments of Inertia of Methyl Bromide.

a. Application of the calorimetric data of Едан and Кемр.

EGAN and KEMP (loc. cit.) determined the entropy of CH₂Br-gas in the ideal state at 1 atm, and 276°.66 K (the boiling point) to 57.86 cal. deg.⁻¹ mol.⁻¹. They estimated the values of A' and C', using the data of Levy and BROCKWAY¹ for the C-Br distance (1.91 + 0.06 Å) and taking C-H equal to 1.09 Å and < H-C-H= 111°. These values correspond to A = 85.3 10^{-40} gcm² and $C = 5.36 \ 10^{-40} \text{ gcm}^2$. Inserting A and C into (V) together with the known vibration frequencies, T, M, and σ (= 3), they calculated the entropy per mole CH₃Br in the ideal gas state at 276°.66 K to 57.99 cal. deg.⁻¹. Thus, good agreement between the calculated and the experimentally determined entropy was found. In the present paper, however, we wish to reverse matters, e.g. exactly to determine the contribution of Egan and Kemp's calorimetric data to our knowledge of the dimensions of the CH₃Br-molecule. As is seen from (V), the calorimetric data determine the product A'2 C'. By combining the value found with spectroscopic results, the best possible values for the moments of inertia of CH₂Br are obtained. These figures will be applied in a paper to be published later. From (V) we obtain:

$$\begin{split} 1/2\ln A'^{2}C' &= \frac{57.86}{R} + \ln 3 - \left(2.307 + 4\ln T + \frac{3}{2}\ln M + \right. \\ &+ \left. \sum_{f=1}^{3n-6} S_{Ein}(\nu_{f}, T) \right). \end{split}$$

The uncertainty of the value 57.86 is \pm 0.1, all other figures are known to be practically exact. This means that

$$A^{2} \cdot C = 33400 \ 10^{-120} g^{3} cm^{6} \pm 10^{0} /_{0}.$$
 (V')

J. Am. Chem. Soc. 59, 1662 (1937).

b. Application of the structure of infrared bands.

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In 1928, BENNETT and MAYER have studied the infrared absorption spectrum of gaseous $CH_3Br.^1$ Parallel bands (||) were found at 610, 1305 and 2972 cm⁻¹, perpendicular bands (\perp) at 956.9. 1450.5 and 3061.5 cm⁻¹. A study of the structure of these bands gives us some information on the size of the molecule.

From the structure of the || bands the absorption maximu of the P- and R-branches could be determined. The distance between the absorption maxima of a single band is called the doublet separation and is denoted by $\delta \nu$. GERHARD and DEN-NISON² have demonstrated that

$$\delta \nu = rac{\mathrm{S}}{\pi} \sqrt{rac{\mathrm{k}\mathrm{T}}{\mathrm{A}}} \qquad \log_{10}\mathrm{S} = rac{0.721}{\left(rac{\mathrm{A}}{\mathrm{C}} + 3
ight)^{1.13}}.$$

 δv is ~ 25 cm⁻¹ and could only be measured with an accuracy in accordance with EGAN and KEMP, we obtain of ~ 2-3 cm⁻¹.

Therefore the average of the following results is taken.

Doublet separation cm^{-1} .

| BENNET and MAYER ³ | 25 23 23 |
|---------------------------------|---------------|
| Moorhead ⁴ | 26 -25 24 |
| Sleator ⁵ | 26 |
| BARKER and NIELSEN ⁶ | 27.5 |

As an average value is used $\delta v = 25.0 \text{ cm}^{-1} \pm 1.0$.

The \perp bands show a rotational fine structure which was resolved by BENNETT and MAYER (loc. cit.). The fine structure is found to be more complicated than usual since the \perp vibrational levels are double-degenerate; this means that an interaction be tween rotational and vibrational movements takes place, disturb

¹ Phys. Rev. **32**, 888 (1928).

² GERHARD and DENNISON, Phys. Rev. 43, 197 (1933).

- ³ BENNETT and MEYER, loc. cit.
- ⁴ MOORHEAD, Phys. Rev. 39, 788 (1932).
- ⁵ SLEATOR, Phys. Rev. 38, 147 (1932).
- ⁶ BARKER and NIELSEN, Phys. Rev. 46, 970 (1934).

ing the usual regularity of the bands. However, DENNISON and JOHNSTON¹ assuming harmonic vibrations, showed that

$$\sum_{1}^{3} \Delta \nu = \frac{h}{4\pi^{2}} \left(\frac{3}{C} - \frac{7}{2A} \right), \qquad (VII)$$

where $\Delta \nu$ is the average line spacing within one of the \perp bands, and $\sum_{1}^{3} \Delta \nu$ is the sum of the average values of all three \perp bands. (VII) mainly determines C, because A ~ 15 C. For a given A, DENNISON and JOHNSTON (loc. cit.) estimated that C may be found with an error of about 5 $^{0}/_{0}$.

c. Numerical calculations.

From (VII) it is seen that only a rough knowledge of A is necessary to obtain a good value of C. Using $A = 85 \cdot 10^{-40} \text{ gcm}^2$ in accordance with EGAN and KEMP, we obtain

$$C = 5.42 \ 10^{-40} \text{ gcm}^2 \pm 5 \ ^{0}/_{0}.$$

An error of 10 $^{0}/_{0}$ in the value assumed for A, only changes C by 1 $^{0}/_{0}$. The calculation is carried through on the basis of $\sum_{1}^{3} \Delta \nu = 28.32 \text{ cm}^{-1}$ from the paper of BENNETT and MAYER (loc. cit.).

Now, by inserting $C = 5.42 \ 10^{-40}$ in (V') and (VI) we get two values of A. Substituting C in (V') and allowing for an error of 5 0/0 in C and 10 0/0 in the calorimetric A²C-value we find

$$A = 78 \cdot 10^{-40} \text{ gcm}^2 \pm 8 \ ^{0}/_{0}.$$

Inserting $C = 5.42 \cdot 10^{-40}$ in (V1), it is seen at once that, as $\Lambda/C \sim 15$, S ~ 1.065. If C changes by 5 $^{0}/_{0}$, S becomes 1.070, *biz.* a change in C within the experimentally permissible limits is of negligible effect on S. Thus, the error of A simply is about wice the error of $\delta \nu$. Consequently we get:

A = $82 \cdot 10^{-40} \text{ gcm}^2 \pm 10^{-6} \text{ o}_{10}$.

¹ DENNISON and JOHNSTON, Phys. Rev. 48, 868 (1935).

According to the above-mentioned results the value of A equally well consistent with calorimetric and with spectroscopic data, is then

A = $80 \cdot 10^{-40} \text{ gcm}^2 \pm 6^{-0}/_{0}$.

In the calculation of $A = 82 \cdot 10^{-40} \text{ gcm}^2$ by means of (VI) and (VII) due regard was paid to the interdependence of rota tional and vibrational energies. In using (VII) and (V') which leads to $A = 78 \cdot 10^{-40} \text{ gcm}^2$, this interdependence is partly ignored. The fact that almost the same values of A are obtained supports the view that the approximation made in formulating (V) is rather good.

VI. Summary.

(1) The expression for the entropy of 1 mole of CH_3Br in the ideal gas state is considered and the derivation from more general expressions is discussed.

(2) The calorimetric data given by EGAN and KEMP are applied to find the product A²C. The infrared measurements of BENNETT and MEYER are used to calculate the value of C. Combining calorimetric and spectroscopic data $A = .78 \cdot 10^{-40}$ gcm² (± 8 per cent) and $C = 5.42 \cdot 10^{-40}$ gcm² (± 5 per cent) is obtained.

Infrared measurements by BENNETT and MEYER, MOORHEAD SLEATOR, BARKER and NIELSEN permit the calculation of A = 82 10^{-40} gcm² (± 10 per cent) on a purely spectroscopical basis.

(3) A value for A, equally well consistent with spectro scopical and heat capacity measurements, is $80 \cdot 10^{-40}$ gcm²

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II. EQUILIBRIUM CONSTANTS OF THE REACTION CH₃Br+HCl ≈ CH₃Cl+HBr MOMENTS OF INERTIA OF METHYL BROMIDE

I. Introduction.

In a previous paper by the present author¹ the formula

$$\frac{R}{2.307 + 4 \ln T + \frac{3}{2} \ln M + \frac{1}{2} \ln A'^{2}C' + \ln \frac{p_{e}p_{n}I}{\sigma} + \sum_{f=1}^{3n-6} S_{Ein}(v_{f}, T) \right]$$
(I)

was shown to be valid in a large temperature interval $(100^{\circ}-1000^{\circ} \text{ K})$ for the entropy of one mole of CH₃Br-gas in the ideal state at 1 atm. It was demonstrated how the measurements of heat capacity by EGAN and KEMP² can be used for finding the product A'²C'. In the present paper it is shown how A' can be determined by measuring another thermodynamical quantity, wiz. the equilibrium constant of the reaction

$CH_3Br + HCl \rightleftharpoons CH_3Cl + HBr$

at various temperatures, the final calculation of A' being based upon the equilibrium constants of the above reaction and spectroscopical data available in the literature.

For the most convenient formulation of the problem (I) is ombined with the general thermodynamical relation

$$G = E - TS + pV, \qquad (1)$$

where the thermodynamical potential G, is defined as a function of the internal energy E, the absolute temperature T, the entropy

¹ D. Kgl. Danske Vidensk. Selskab, Mat.-fys. Medd. XXIV, 9. Here cited (S-TI). ³ J. Am. Chem. Soc. **60**, 2097 (1938).

S, the pressure p, and the volume V. As only ideal gases are considered pV = RT. Furthermore, $E^{\circ} = E_0^{\circ} + \frac{3}{2}RT + RT^2 \frac{d\ln \cdot Z}{dT}$ where E_0° is the internal energy at the absolute zero, $\frac{3}{2}$ RT is the translational energy, and the last term is the energy due to all other degrees of freedom (electronic, vibrational, etc.). This equation is easy to derive by means of Table I, (S-TI). Substituting for E° in (1) we get

$$\mathrm{G}^\circ = \mathrm{E}^\circ_0 + \frac{5}{2}\mathrm{R}\mathrm{T} - \mathrm{T}\mathrm{S}^\circ + \mathrm{R}\mathrm{T}^2 \frac{\mathrm{d}\mathrm{ln}\mathrm{Z}}{\mathrm{d}\mathrm{T}}.$$

As already shown (S-TI), Z can be written as $Z_{vib} \cdot Z_{rot}$, which means that

$$\frac{\mathrm{dln}Z}{\mathrm{d}T} = \frac{\mathrm{dln}Z_{\mathrm{vib}}}{\mathrm{d}T} + \frac{\mathrm{dln}Z_{\mathrm{rot}}}{\mathrm{d}T}.$$

But

$$RT^{2}\frac{dlnZ_{vib}}{dT} = RT\sum_{t=1}^{3n-6} \frac{\frac{\varepsilon_{t}}{kT}}{\frac{\varepsilon_{r}}{e^{kT}-1}} \quad and \quad RT^{2}\frac{dlnZ_{rot}}{dT} = \frac{3}{2}RT.$$

Substituting for Z in (2) we get

$$\frac{\mathbf{S}^{\circ} - \mathbf{E}_{0}^{\circ}}{\mathbf{T}} = \mathbf{R} \left[4 - \frac{\mathbf{S}^{\circ}}{\mathbf{R}} + \sum_{\mathbf{f}=\mathbf{1}}^{\mathbf{3n-6}} \frac{\frac{\varepsilon_{\mathbf{f}}}{\mathbf{kT}}}{\frac{\varepsilon_{t}}{\mathbf{kT}} - 1} \right]^{\circ}$$

Introducing the value of S given by (I) we derive

$$\frac{G^{\circ} - E_{0}^{\circ}}{T} = R \left[1.694 - 4 \ln T - \frac{3}{2} \ln M - \frac{1}{2} \ln A'^{2} C' + 1 \ln 3 + \sum_{f=1}^{3n-6} \ln \left(1 - e^{\frac{-\varepsilon_{f}}{kT}} \right) \right].$$

Now, we want to form $\Delta \frac{G^{\circ} - E_{0}^{\circ}}{T}$ for the reaction $CH_{3}Br$ $HCl = CH_{3}Cl + HBr$. The part of the function originating from the conversion of CH₃Br into CH₃Cl is easily seen to be

$$\mathbb{R}\left[\frac{3}{2}\ln\frac{M\left(CH_{3}Br\right)}{M\left(CH_{3}Cl\right)} + \ln\frac{A'\left(CH_{3}Br\right)}{A'\left(CH_{3}Cl\right)} + \sum_{f=1}^{3n-6}\ln\left(1-e^{\frac{-\varepsilon_{f}}{kT}}\right) - \sum_{f=1}^{3n-6}\ln\left(1-e^{\frac{-\varepsilon_{f}}{kT}}\right)\right]$$

$$(5)$$

Here, M(CH₃Y) is the molecular weight of the molecule CH₃Y, and A'(CH₈Y) is $10^{38} \times$ the moment of inertia of the molecule with respect to an axis perpendicular to the C-Y bond through the centre of gravity. The term

$$\ln \cdot \frac{C'(CH_{3}Br)}{C'(CH_{3}Cl)}$$

has been put equal to zero. Experimentally C'(CH₂Br) was found to be 0.0542, viz. the same as for CH_4 .¹ Using the same experimental method, C'(CH₃Cl) is found to be 0.0544. However, both values have an uncertainty of 5 per cent, but the deviations from $C'(CH_{4})$ must have the same sign and be very nearly equal. Thus $C'(CH_3Br) = C'(CH_3Cl)$.

The part of the function $\Delta \frac{G^{\circ} - E_{0}^{\circ}}{T}$ originating from the conversion of HCl into HBr is found from tables available in the literature.² In Table I values of $-\frac{G^{\circ}-E_{0}^{\circ}}{T}$ for HBr and HCl are given.

Table I.

Values of $-\frac{G^{\circ}-E_{0}^{\circ}}{T}$ for HBr and HCl. $(cal. deg.^{-1} mole^{-1})$

| Abs. temp | 250 | 300 | 400 | 500 | 600 | 700 | 800 | 900 | 1000 |
|------------|------------------|------------------|------------------|------------------|--------------------|------------------|------------------|--------------------|------------------|
| HBr | 39.330 36.487 | 40.594 37.778 | 42.589 39.771 | 44.139 41.321 | $45.409 \\ 42.588$ | 46.487 43.663 | 47.426 44.597 | $48.259 \\ 45.425$ | 49.019 46.171 |
| Difference | 2.843 | 2.816 | 2.818 | 2.818 | 2.821 | 2.824 | 2.829 | 2.834 | 2.839 |
| | - | | | | | | | | |

¹ S-T I, p. 9—10.

(2)

Gordon and Barnes, Journ. Chem. Phys. (1), 692 (1933); GIAUQUE, J. Am. em. Soc. 54, 1731 (1932). Kgl. Danske Vidensk. Selskab, Mat.-fys. Medd. XXIV, 9.

 $\mathbf{2}$

2*

interval 350° K-600° K. Table I shows that in this interval the ratio $\Delta \frac{G^{\circ} - E_{0}^{\circ}}{T}$ originating from HCl \rightarrow HBr can with good approxim ation be put equal to -2.819 cal. deg.⁻¹ mole⁻¹.

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Consequently we get for the reaction $CH_3Br + HCl \rightarrow CH_3Cl$ + HBr

$$\begin{split} & \Delta \frac{\mathrm{G}^{\circ} - \mathrm{E}^{\circ}_{0}}{\mathrm{T}} = \mathrm{R} \left[\frac{3}{2} \ln \frac{\mathrm{M} \left(\mathrm{CH}_{3} \mathrm{Br} \right)}{\mathrm{M} \left(\mathrm{CH}_{3} \mathrm{Cl} \right)} + \ln \frac{\mathrm{A}^{\prime} \left(\mathrm{CH}_{3} \mathrm{Br} \right)}{\mathrm{A}^{\prime} \left(\mathrm{CH}_{3} \mathrm{Cl} \right)} + \right. \\ & + \sum_{\mathrm{I} = 1}^{\mathrm{3n-6}} \ln \left(1 - \mathrm{e}^{\frac{-\varepsilon_{\mathrm{I}}}{\mathrm{kT}}} \right) - \sum_{\mathrm{I} = 1}^{\mathrm{3n-6}} \ln \left(1 - \mathrm{e}^{\frac{-\varepsilon_{\mathrm{I}}}{\mathrm{kT}}} \right) - \frac{2.819}{\mathrm{R}} \right]. \end{split}$$

The general relation between the ΔG of a given reaction and the equilibrium constant for the corresponding equilibrium is

 $\angle G = -RTlnk$,

where k or k (T), as it will often be written, is the thermodynamic equilibrium constant. Combining this relation with (6) we get

$$k\left(T\right) = \left(\frac{M\left(CH_{3}Cl\right)}{M\left(CH_{3}Br\right)}\right)^{\prime\prime_{z}} \frac{A'\left(CH_{3}Cl\right)}{A'\left(CH_{3}Br\right)} \frac{\int_{t=1}^{3n-6} \left(1 - e^{\frac{-\epsilon_{t}}{kT}}\right)_{CH_{3}Br}}{\int_{t=1}^{3n-6} \left(1 - e^{\frac{-\epsilon_{t}}{kT}}\right)_{CH_{3}Cl}} e^{\frac{2.819}{R} - \frac{\Delta E_{s}^{*}}{RT}}$$

If the equilibrium constants at two different temperatures are known, the knowledge of the quantity $\varDelta E_0^\circ$ is unnecessary to our purpose (8):

$$\frac{\mathbf{k} \left(\mathbf{T}_{1}\right)^{\frac{\mathbf{T}_{1} - \mathbf{T}_{s}}{\mathbf{T}_{1} - \mathbf{T}_{s}}}}{\mathbf{k} \left(\mathbf{T}_{2}\right)^{\frac{\mathbf{T}_{1} - \mathbf{T}_{s}}{\mathbf{T}_{t} - \mathbf{T}_{s}}} = \mathbf{e}^{\frac{2.819}{\mathbf{R}}} \left(\frac{\mathbf{M} \left(\mathbf{CH}_{3}\mathbf{Cl}\right)}{\mathbf{M} \left(\mathbf{CH}_{3}\mathbf{Br}\right)}\right)^{3/2} \frac{\mathbf{A}' \left(\mathbf{CH}_{3}\mathbf{Cl}\right)}{\mathbf{A}' \left(\mathbf{CH}_{3}\mathbf{Br}\right)} \cdot \\ \cdot \left[\frac{3n^{-6}}{\prod_{t=1}^{t} \left(1 - e^{\frac{\epsilon_{t}}{\mathbf{k} \mathbf{T}_{s}}}\right)_{\mathbf{CH}_{s}\mathbf{Br}}}{\prod_{t=1}^{T_{1} - \mathbf{T}_{s}}}\right]^{\frac{\mathbf{T}_{1}}{\mathbf{T}_{1} - \mathbf{T}_{s}}} \left[\frac{3n^{-6}}{\prod_{t=1}^{t} \left(1 - e^{\frac{\epsilon_{t}}{\mathbf{k} \mathbf{T}_{s}}}\right)_{\mathbf{CH}_{s}\mathbf{Cl}}}{\prod_{t=1}^{T_{1} - \mathbf{T}_{s}}}\right]^{\frac{\mathbf{T}_{1}}{\mathbf{T}_{1} - \mathbf{T}_{s}}} \left[\frac{3n^{-6} \left(1 - e^{\frac{-\epsilon_{t}}{\mathbf{k} \mathbf{T}_{s}}}\right)_{\mathbf{CH}_{s}\mathbf{Cl}}}{\prod_{t=1}^{T_{1} - \mathbf{T}_{s}} \left(1 - e^{\frac{-\epsilon_{t}}{\mathbf{k} \mathbf{T}_{s}}}\right)_{\mathbf{CH}_{s}\mathbf{Br}}\right]^{\frac{\mathbf{T}_{s}}{\mathbf{T}_{s}}}\right]^{\frac{\mathbf{T}_{s}}{\mathbf{T}_{s}}} \left[\frac{3n^{-6} \left(1 - e^{\frac{-\epsilon_{t}}{\mathbf{k} \mathbf{T}_{s}}}\right)_{\mathbf{CH}_{s}\mathbf{Cl}}}{\prod_{t=1}^{T_{1} - \mathbf{T}_{s}} \left(1 - e^{\frac{-\epsilon_{t}}{\mathbf{k} \mathbf{T}_{s}}}\right)_{\mathbf{CH}_{s}\mathbf{Br}}}\right]^{\frac{\mathbf{T}_{s}}{\mathbf{T}_{s}}}\right]^{\frac{\mathbf{T}_{s}}{\mathbf{T}_{s}}}$$

The equilibrium in question was studied in the temperature Thus, by means of equilibrium data and spectroscopical data

$$\frac{A'(CH_{3}Cl)}{A'(CH_{3}Br)}$$

can be calculated. From the fairly accurate value of A'(CH₃Cl), known from work in the infrared by NIELSEN,¹ A'(CH₃Br) can be calculated.²

I. Experimental Determination of the Equilibrium Constant at Different Temperatures.

a. Preparation of CH₃Br.

Commercial bromine was freed from chlorine by being kept 24 hours in contact with an aqueous solution of KBr under shaking at intervals. Subsequently the bromine was distilled off and reduced to HBr by means of SO₂ in the usual way, a constantly boiling hydrobromic acid being prepared. By heating the hydrobromic acid to 70° C and adding methyl alcohol a gentle evolution of gaseous CH₃Br is obtained. The gas is fractionated through a column, jacketed with water, at 5° C, led through 3 wash-bottles with water and 3 with concentrated sulphuric acid and is finally condensed. Its purity was checked by its Raman pectrum. Since the spectrum showed no lines originating from ater, methyl alcohol, dimethyl ether, methyl chloride, or any ther compound, the sample contains no water or methyl alcohol, such substances being very easily detectable in the Raman spectrum. Dimethyl ether and methyl chloride must be present amounts of less than c. $\frac{1}{2}$ per cent and, actually, the way preparing the sample makes it highly probable that it is even ss: Unfortunately the constancy of the melting point and the urse of the premelting curve could not be studied.

The CH₃Br was kept in a glass vessel, M (fig. 1), surrounded nce. Prior to each experiment c. 1 g was distilled from M to (or T₂), which was placed in liquid air. Then a high vacuum s established and the CH₃Br was twice sublimated from T₁ , and vice-versa. At the end of each sublimation the last tenth was pumped off. This treatment ensures the presence

Nielsen, Phys. Rev. 56, 847 (1939). Compare, however, the note added in proof. of an air-free sample, which was afterwards allowed to distint that part of the apparatus (A), where the amount of CH_3B_5 was determined.

b. Preparation of HCl.

While a suitable amount of CH_3Br was prepared for a whole series of experiments, HCl was produced for each single de termination of the equilibrium. Conc. hydrochloric acid (0.5 0.7 cc) was added to 400 cc conc. $H_2SO_4^{-1}$ in a carfully evacuated flask through a separatory funnel, the tube of which was led to the bottom of the sulphuric acid (H, fig. 1). When the stopcock of the separatory funnel is cautiously opened the hydrochloric acid distils to the bottom of the conc. sulphuric acid, and a stream of dry HCl is obtained. The gas is condensed in T_1 or T_2 . Before using it in the experiment it is subjected to the same treatment as CH_3Br (sublimation *in vacuo*). In this way an air- and water-free sample of HCl was prepared as will be seen from experiments referred to under d.

The pink, crystalline modification of HCl, noticed by GREM and BURT² and by GIAUQUE and WIEBE³ was again observed.

c. Determination of the amount of CH₃Br used in the experiments.

From the evacuated tube T_1 (or T_2) CH₃Br was distilled int an evacuated 1 l-bulb A, placed in a thermostat. After 2 hours the pressure of the gas was read off by means of the mercurs manometer P. A Dewar vessel with liquid air was put around the evacuated tube B until all CH₃Br was condensed. Now, a series of preliminary experiments, the tube B was carefully sealed off, washed outside with ethyl alcohol and dried *in vacu* over P_2O_5 . The weight of the tube was determined on the analytic balance. Subsequently, the tube was broken by being scratched cautiously and heated in a little (2 mm) flame. In this way tube can be opened with practically no loss of solid material blanks have shown. The tube was again dried *in vacuo* and weighed Its volume was determined by its water content being weighe

- ² Journ, Chem. Soc. Lond., 1669 (1909).
- ³ Journ. Am. Chem. Soc. 50, 101 (1928).



¹ This amount suffices for abt. 20 preparations of 0.01 mole dry HCL

In this manner the amount of CH₃Br in grams corresponding a certain manometer reading was determined. By carrying on a great number of similar experiments an equation, giving the number of moles CH₃Br in A as a function of the manometer reading, was found (y mole $CH_3Br = 0.00006051 \text{ x} - 0.000031$ where x is the cathetometer reading in mm at a temperature the mercury of 19°C). Thus, in equilibrium experiments, the analytical expression and a manometer reading serve as practical means of finding the amount of CH₃Br involved the reaction.

The manometer readings were taken by means of a cathe tometer. Each pressure was determined as the average of the cathetometer readings. In this way the pressure determination exact to about ¹/₄ per thousand for the pressures in question viz. 100 mm Hg. The pressure reading and the use of y-equation together cause an uncertainty in the determination of the amount of CH₃Br to c. 0.2 per cent.

At the thermostat temperature and a pressure of 100 m Hg CH₃Br does not obey the ideal gas law. In view of the general interest of this fact the respective experimental data are give in Table II.

| Deviation of origon from the rate of the | | | | | | | | | | |
|--|--------|------------------|-------------------|-----------|--|--|--|--|--|--|
| g CH ₃ Br | p atm. | pv liter-atm. | nRT liter-atm. | nRT pv | | | | | | |
| | | <u> </u> | | | | | | | | |
| 0.7685 | 0,1764 | 0.1950 | 0.1961 | 1.005 | | | | | | |
| 0.7085 | 0.1625 | 0.1796 | 0.1808 | 1.006 | | | | | | |
| 0.6499 | 0.1490 | 0.1647 | 0.1658 | 1.006 | | | | | | |

0.1363

0.1197

0.1076

0.5934

0.5202

0.4677

Table II. Deviation of CH Br from the ideal gas state.

> 0.1189 Volume of A: 1.10551 at 295.2° K $\pm 0.1^{\circ}$.

0.1507

0.1323

d. Determination of the amount of HCl used in the experiments.

The amount of HCl present in A could not be determine in the same way as in the case of CH₃Br due to the high press developing in the ampulla when heated to room temperate

in these experiments, therefore, B was connected with the remaining apparatus by means of a ground glass joint, which permits removing B after condensation of the HCl gas. In a stream hydrogen the HCl was subsequently distilled into water, which issolves HCl quantitatively. Cl was precipitated as AgCl, which was filtered off and dried to constant weight. In this way an quation giving the dependence between the pressure reading and the number of moles HCl in A was obtained (z mole HCl =000005883 x + 0.000101, where x is the cathetometer reading as the case of CH₃Br).

GREY and BURT¹ have shown that at p = 180 mm Hg and for temperature nRT = 1.0012. At the somewhat lower presure (100 mm) used in our experiment, the gas must be practically deal. If, in our experiment, this result can be reproduced, it icans that the HCl prepared as described under b must be pure. The results of 5 experiments are given in Table III.

Table III.

Proof that the HCl-gas used obeys the ideal gas law.

| C1 | Corresp. g HCl | p atm. | pv liter-atm. | nRT liter-atm. | $\frac{nRT}{pv}$ |
|----|---|--------|------------------|-------------------|------------------|
| 93 | $\begin{array}{c} 0.3000 \\ 0.2978 \\ 0.2681 \\ 0.2531 \\ 0.2293 \end{array}$ | 0.1807 | 0.1997 | 0.1993 | 0.998 |
| 06 | | 0.1790 | 0.1978 | 0.1979 | 1.001 |
| 39 | | 0.1610 | 0.1778 | 0.1781 | 1.002 |
| 52 | | 0.1519 | 0.1678 | 0.1682 | 1.002 |
| 15 | | 0.1377 | 0.1521 | 0.1523 | 1.001 |

Volume of A: 1.10551 at $295.2 \pm 0.1^{\circ}$ K.

1.17

1.005

1.003

1.003

0.1514

0.1327

0.1193

e. The reaction vessel.

After successive determinations of the gas quantities in A and econdensation in B of CH₃Br and HCl, the Dewar vessel with and air was removed from B, which results in the evaporation the two gases into the reaction vessel C (fig. 1). The vessel as a 31-bulb of pyrex glass, surrounded by two tightly-fitting opper hemispheres. These hemispheres were surrounded by a ser of asbestos paper and asbestos wool together with an electrical using wire. The whole arrangement was again surrounded by Journ. Chem. Soc. Lond., 1669 (1909).

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thermocouples were placed at t_1, t_2 , and t_3 . In this way it was possible to maintain temperatures deviating less than 2°, t₂ gener ally being very nearly the mean of t₁ and t₃. No thermo-regulate was necessary for keeping the temperature constant within during an experiment. By varying the heating current any desired temperature between 20° C and 450° C could be obtained.

The thermocouples were calibrated in the vapors of boiling benzene, water, toluene, bromobenzene, naphtalene, benzophene and mercury. At 350°C the reading is accurate to 0.5°, at 100% it is accurate to 0.2° .

f. Analytical determination of the position of the equilibrium.

After equilibrium had been established in C, the equilibrium mixture was frozen down into the carefully evacuated trap surrounded by liquid air. After 2 hours the stopcock S was closed. By means of a stream of hydrogen the reaction mixture was passed through 75 cc water in an 300 cc Erlenmeyer flast HBr and HCl are dissolved quantitatively in water. Most of the CH₃Br and CH₃Cl is passing, as blanks have shown, the rest removed by continued bubbling-through of hydrogen for 2 hour In a special experiment it was shown, moreover, that neither CH,R nor CH₃Cl hydrolyse under the present circumstances.

The amount of acid was determined by titration with 0.5 NaOH. Blank experiments with HCl alone prove that the quantity of acid found by means of this titration is in excellent agreement with the amount calculated by means of the equation mentioned under d.

Using the mass-law of action for the equilibrium we obtain

 \mathbf{mc}

 $c(m-\alpha) c(1-\alpha)$

 $CH_{3}Br + HCl \rightleftharpoons CH_{3}Cl + HBr$

 $c\alpha$

ca

Number of moles before reaction:

Number of moles in the

equilibrium:

$$k = \frac{a^2}{(m-a)(1-a)}.$$

a big tin container, filled with kieselguhr. Copper-constantate m is the known ratio between the number of moles CH₃Br and HCl before the reaction. If the ratio between HBr and HCl in the equilibrium is f, a is given by $f = \frac{1-a}{a}$. Consequently a determination of the ratio between $\overline{B}r$ and $\overline{C}l$ in the aqueous solution of HBr + HCl must be made.

> This special problem has been studied by several authors. See e.g. GMELIN, Handb. der anorg. Chem.). I have checked a series of these methods. The method described by LANG¹ M_{0x} in the presence of HCN and $H_{3}PO_{4}$, reduction of surplus $KMnO_4$ by $FeSO_4$, addition of KJ and thration with $Na_2S_2O_3$) was found to be of suitable accuracy and convenience. By this method the contents of $\overline{B}r$ can be determined almost independently of the contents of $\overline{C}l$. In the present experiments we are interested in determining Br in the presence of 3–5 times as much \overline{Cl} . Table IV gives the results of using Lang's method on weighed quantities of KBr and KCl.

| Τa | b | 1 | e | Ι | v | |
|----|---|---|---|---|---|--|
| | | | | | | |

| g KBr | Equiv. Br. | g KCl | Equiv. Cl. | $\frac{\overline{B}r}{\overline{C}l}$ | Equiv. Br. found. | Error |
|--------|------------|--------|------------|---------------------------------------|----------------------|---------------------|
| 0.2029 | 0.001704 | 0.5025 | 0.006740 | 0.252 | 0.001721 | 1.0 °/ ₀ |
| 0.1943 | 0.001632 | 0.5047 | 0.006769 | 0.241 | 0.001649 | 1.0 °/ ₀ |
| 0.1460 | 0.001226 | 0.5103 | 0.006844 | 0.179 | 0.001239 | 1.1 °/ ₀ |
| 0.1277 | 0.001073 | 0.4973 | 0.006670 | 0.161 | 0.001085 | 1.2 °/ ₀ |

Lang's method thus gives reproduceable, although not quite correct values for the $\overline{\mathrm{Br}}$ contents. In practice, the thiosulphate solution used was adjusted to solutions of KBr + KCl, almost It is the those to be analyzed. In this way the amount of $\overline{B}r$ can be found with an accuracy of about 0.3 per cent.

The inaccuracy in the determination of m and f is seen to cause an inaccuracy of k of about 1.5-2 per cent, as verified by equilibrium experiments.

The determination of the equilibrium constant at 606°K in the absence of a catalyst.

As seen from the preceding sections, the equilibrium was udied by mixing known amounts of CH₃Br and HCl in 'C' and Zeitsch. f. anorg. u. allg. Chemie 144, 75 (1925).

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heating the mixture. As preliminary experiments show, the exchange of Br and Cl starts at 250-300° C in the absence of a catalyst. At 330-340° C, equilibrium is established within 40-50 hours. Some experiments aiming at a faster establishment of the equilibrium were carried out at higher temperatures. At 390°C the following observations were made: After 40 hours the reaction mixture was led to the trap D. The condensation, being complete in corresponding experiments at 330° C, now was incomplete At the same time the number of equivalents of acid, present in D after the reaction, exceeded the number present before the reaction. Thus, some 'side reaction' must take place, because all the reaction partners of the equilibrium CH₂Br + HCl $CH_{3}Cl + HBr$, are condensable and the number of equivalents of acid is constant. In fact, the only compound which could not be condensed in liquid air and which could be formed from the reaction partners, is hydrogen. When, in a following experiment HCI was omitted, the contents of 'C' were likewise not completely condensable in D after 24 hours, a considerable amount of HB (c. 0.1 mole per cent) being simultaneously formed. This in dicates that the 'side reaction' probably is

Nr. 9

Nr. 9

$\begin{array}{c} \mathrm{CH_{2}Br} \\ 2 \ \mathrm{CH_{3}Br} \rightarrow \mathrm{H_{2}+} \mid \\ \mathrm{CH_{2}Br} \end{array}$

HBr being produced by subsequent reactions such as

$$\begin{array}{ccc} CH_2Br & CHBr & CH_2Br & CH_3\\ | & \rightarrow HBr + \parallel & \text{or} & | & +H_2 \rightarrow | & +HBr \\ CH_2Br & CH_2 & CH_2Br & CH_2Br & \end{array}$$

At 330° C, however, the condensation in D was complete an no extra equivalents of acid were formed. To ensure that ro secondary reactions take place in experiments at this temperature an experiment with 0.01 mole CH₃Br alone was run for 10 days 330° C. The subsequent condensation in D was complete and no HBr was formed. In a similar experiment with 0.05 mole CH₃Br the condensate in D was distilled into a Raman tube and th Raman spectrum was photographed. The spectrum showed in signs of other lines than those corresponding to CH₃Br. If e

CH₂BrCH₂Br had been present it would have been particularly easy to detect because of the isolated Raman line of the C—C bond. Consequently it was decided to carry out a series of determinations of the equilibrium constant at some temperature between 330 and 340° C. The results are given in table V.

Table V. Equilibrium constant determinations at 606°K.

| Duratio (hours) | Equiv. CH ₃ Br. before exper. | Equiv. HCl before exper. | m | Equiv. HCl + HBr aft. exp. | Equiv. HBr after exper. | f | α | $\left \frac{a^2}{(m-a)(1-a)}\right $ |
|--------------------|---|-----------------------------------|--------|-------------------------------------|----------------------------------|--------|--------|---------------------------------------|
| 00.1 | | | _ | · · · | | | | |
| 22 hour | s 0.007891 | 0.007986 | 0.9882 | 0.007996 | 0.001975 | 0.3280 | 0.2470 | 0.1093 |
| 46 — | 0.007786 | 0.006162 | 1.2635 | 0.006162 | 0.001845 | 0.4274 | 0.2994 | 0.1327 |
| 64 — | 0.007121 | 0.007146 | 0.9965 | 0.007131 | 0.001916 | 0.3674 | 0.2687 | 0.1356 |
| (93 — | 0.007125 | 0.007381 | 0.9653 | 0.007377 | 0.001947 | 0.3586 | 0.2639 | 0.1349 |
| 112 — | 0.007200 | 0.007007 | 1.0275 | 0.006982 | 0.001896 | 0.3728 | 0.2716 | 0.1340 |
| 141 — | 0.006522 | 0.008077 | 0.8074 | 0.008087 | 0.001951 | 0.3180 | 0.2413 | 0.1355 |
| 72 — | 0.007863 | 0.007767 | 1.0123 | 0.007767 | 0.002096 | 0.3696 | 0.2698 | 0.1342 |
| 72 — | 0.007797 | 0.006774 | 1.1510 | 0.006781 | 0.001965 | 0.4080 | 0.2898 | 0.1373 |
| 67 — | 0.006704 | 0.007587 | 0.8836 | 0.007578 | 0.001918 | 0.3389 | 0.2531 | 0.1360 |
| 63 | 0.007791 | 0.006341 | 1.2286 | 0.006334 | 0.001890 | 0,4253 | 0.2984 | 0.1364 |

Mean of experiments 2-10: 0.1352. Result: $0.1352 \pm 0.0008 = k$.

In connexion with Table V the use of the mass-law of action may be discussed. The law is only fulfilled for ideal gases. At higher temperatures and lower pressure, the actual gases can be considered ideal with better and better approximation. As HCl and HBr are already ideal at p = 150 mm Hg and room temperature they are even more so at the pressure of the experiment (50—100 mm Hg) and the temperatures 80° — 340° C. Table II shows that at room temperature CH_3Br deviates a little from ideality. The same is probably the case with CH_3Cl . At the higher temperatures of the experiments the deviations from ideality are minor. Thus, the ratio between the activities of CH_3Br and CH_3Cl as a good approximation must be equal to the ratio between the concentrations. The application of the mass-law of action must be permissible.

Nr. 9 Nr. 9

h. Determinations of the equilibrium constant at 357°K in the presence of a catalyst.

For the determination of the equilibrium at a temperature as far as possible from 606° K a suitable catalyst was looked for. The first attempt with granulated active carbon turned out to be successful. The catalyst was suspended in a glass spiral in the centre of C (fig. 1). In the presence of this catalyst it is possible to study the equilibrium even at 80° C.

The first experiment with the catalyst was made at the same temperature as the experiments without a catalyst, 606° K. The experiment lasted for 24 hours. After that time the condensation in the trap D was incomplete and the number of equivalents of acid had increased. Thus, some side reaction is catalyzed, too. In the following experiment at the same temperature, which was interrupted after one hour, the condensation in D was nearly complete and the number of equivalents of acid had only in creased by 0.5 per cent. When calculating the equilibrium constant on the assumption that no side reaction had taken place k was found to be 0.1300. Without a catalyst k = 0.1352. In broad outline these experiments indicate that active carbon is an excellent catalyst for the reaction we want to study. Since however, also the side reactions are catalyzed it is impossible to study the equilibrium with and without a catalyst at the same temperature.

Next the highest possible temperature at which the side reactions are negligible was looked for. In experiments at 533° K and 497° K, excess equivalents of acid were formed in the course of 40 hours. At 458° K no excess equivalents of acid were produced during 40 hours. At 419° K the same result was found. Thus experiments with the catalyst at temperatures lower than about 450° K (177° C) can be performed without the complications originating from the side reactions.

Finally the lowest possible temperature at which the equilibrium can conveniently be studied was sought for. At 357° K (84° C) equilibrium is established in the course of 30—40 hours As this is a suitable period, the experiments of Table VI were carried out at that temperature.

| | | Table VI. | | | |
|---------------|--------|-------------|----------|----|-------|
| Determination | of the | equilibrium | constant | at | 357°K |

| < 1 | | | 1 | | | | | | |
|-----|---------------------------|--|-----------------------------------|--------|--------------------------------------|-----------------------------|--------|-----------|--------------------------|
| | Du- ration. (hours) | Equiv. CH ₃ Br before exper. | Equiv. HCl before exper. | , m | Equiv. HBr + HCl after exp. | Equiv. HBr after exp. | f | a | $\frac{a^2}{(1-a)(1-a)}$ |
| | 20 | 0.006295 | 0.000070 | 0.0400 | | | | | |
| 2 | 40 | 0.000335 | 0.006678 | 0.9486 | 0.006647 | 0.001003 | 0.1777 | 0.1509 | 0.03366 |
| | 39 | 0.006730 | 0.006376 | 1.0555 | 0.006376 | 0.001027 | 0.1920 | 0.1611 | 0.03459 |
| 1 | 45 | 0.007021 | 0.006696 | 1.0485 | 0.006685 | 0.001070 | 0.1906 | 0 1601 | 0.03435 |
| | 42 | 0.006264 | 0.007147 | 0.8888 | 0.007126 | 0.001035 | 0 1728 | 0 1 4 7 9 | 0.02421 |
| | 64 | 0.006270 | 0.006782 | 0 9245 | 0.006775 | 0.001001 | 0.1740 | 0.1475 | 0.03431 |
| | 40 | 0.007167 | 0.000702 | 0.0240 | 0.000775 | 0.001021 | 0.1774 | 0.1507 | 0.34560 |
| | 40 | 0.007107 | 0.000010 | 1.1000 | 0.006510 | 0.001070 | 0.1967 | 0.1644 | 0.03457 |
| 1.1 | 40 | 0.006724 | 0.007328 | 0.9230 | 0.007325 | 0.001101 | 0.1769 | 0.1503 | 0.03441 |
| | 40 | 0.006247 | 0.006649 | 0.9395 | 0.006623 | 0.000998 | 0.1774 | 0.1507 | 0.03300 |
| | 43 | 0.006635 | 0.007017 | 0.9455 | 0.007025 | 0.001063 | 0.1783 | 0.1513 | 0.03396 |

Mean number of experiments 2-9: 0.03433. Result: $k = 0.03433 \pm 0.00014$.

III. Calculation of Spectroscopically and Thermodynamically Important Quantities.

a. Calculation of the greatest moment of inertia of CH₃Br.

Formula (8) shows that sufficient data are now available to calculate A' (CH₃Br), the greatest moment of inertia of CH₃Br. Putting $T_1 = 606^{\circ} \text{ K} \pm 1.0^{\circ}$, $T_2 = 357^{\circ} \text{ K} \pm 0.5^{\circ}$ and A' (CH₃Cl) = 0.579¹ and using the vibration data of BENNETT and MAYER² we obtain

 $A' (CH_3Br) = 0.782 \text{ gcm}^2 \pm 4 \text{ per cent.}$

As A' $(CH_3Br) = A (CH_3Br) \cdot 10^{38}$, where A (CH_3Br) is the true moment of inertia, we get

 $75 \cdot 10^{-40} \text{ gcm}^2 < A (CH_3 Br) < 81 \cdot 10^{-40} \text{ gcm}^2.$

This value is in excellent agreement with values found by previous authors (S-TI, p. 13).

¹ NIBLSEN, Phys. Rev. 56, 847 (1939). Compare the note added in proof. ³ BENNETT and MAYER, Phys. Rev. 32, 888 (1928)

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The limits given for the value of A (CH₃Br) were calculated on the assumption that the sources of experimental error are exclusively to be found in the temperature measurements and the analytical determination of the equilibrium. To check the correctness of this we may determine the equilibrium at a third temperature, as different as possible from 357° K and 606° K. On page 28 it was mentioned that the equilibrium in question can be established at 458° K in the presence of the catalyst without side reactions. A temperature of 443° K (170° C) was chosen for the experiment. Two determinations were made.

Determination of the equilibrium at 443° K.

 1. experiment. Duration 36 hours
 k = 0.06610

 2. experiment.
 67 k = 0.06643

 Mean number:
 $k = 0.06636 \pm 0.00100$

Now, calculating A (CH₃Br) by means of the results at 606° K and 443° K we obtain

A (CH₃Br) =
$$70 \cdot 10^{-40}$$
 gcm² ± 8 per cent.

The agreement between the two values found by the present 'equilibrium method' is not quite so satisfactory as was expected. This might mean that some systematic error was neglected. As no such error seems to have occurred in the experimental determination of the equilibrium constants it seems natural to reconsider the theoretical basis. In the derivation of equation (I) the simplifying, partly uncontrollable assumption was made that the interaction between the rotational and vibrational movements of the molecule can be neglected. For the methyl halides it is known with certainty that such interaction occurs. Unfortunately it is very difficult, if not impossible at present, to see to what extent such interaction will influence equations (I) and (8).

Paying due regard to both determinations of A (CH₃Br) made in this paper, we get:

A (CH₃Br) =
$$76.5 \cdot 10^{-40}$$
 gcm² ± 4 per cent.

Even if a systematic error of 5 per cent is taken into account the value found by the present 'equilibrium method' is of the

same accuracy as the values hitherto determined by spectroscopical or physico-chemical methods.

| Spectroscopical methods | $82 \cdot 10^{-40}$ | gcm ² | ± | 10 | per cent. |
|----------------------------|-----------------------|------------------|-------|----|-----------|
| Heat capacity measurements | $78 \cdot 10^{-40}$ | - | \pm | 8 | |
| Equilibrium method' | $76.5 \cdot 10^{-40}$ | _ | ± | 4 | |

The value, equally well conceivable with spectroscopical heat capacity and equilibrium measurements, is:

 $A(CH_{3}Br) = 77.5 \cdot 10^{-40} \pm 4$ per cent.

b. Calculation of ΔE_0° and the heat of reaction different temperatures.¹

From (7) it follows that

$$\frac{JE_{e}^{\circ}}{e^{RT}} = e^{\frac{2.819}{R}} \left(\frac{M(CH_{3}Cl)}{M(CH_{3}Br)}\right)^{3/2} \frac{A'(CH_{3}Cl)}{A'(CH_{3}Br)} \frac{\int_{f=1}^{3n-6} \left(1 - e^{\frac{-\varepsilon_{f}}{kT}}\right)_{CH_{3}Br}}{\int_{f=1}^{3n-6} \left(1 - e^{\frac{-\varepsilon_{f}}{kT}}\right)_{CH_{3}Cl}} k(T)^{-1}.$$
(9)

As all the quantities of the right-hand side are known, we can calculate:

$$\Delta E_0^\circ = 2500 \text{ gcalmole}^{-1} \pm 75.$$

The enthalpy H, the thermodynamical potential G, the entropy S, and the temperature T are connected by the relation:

$$\mathbf{H} = \mathbf{G} + \mathbf{TS}.$$

Taking the value of G from (3) we get:

$$\mathrm{H}^{\circ} = \mathrm{E}_{0}^{\circ} + \mathrm{RT} \left(4 + \sum_{\mathrm{f}=1}^{3\mathrm{n}-6} \frac{\frac{\varepsilon_{\mathrm{f}}}{\mathrm{kT}}}{\frac{\varepsilon_{\mathrm{f}}}{\mathrm{e}^{\mathrm{kT}}} - 1} \right).$$

¹ In the newest American literature ΔH_0° is were commonly used for ΔE_0° .

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We now want to calculate ΔH° for the reaction $CH_3Br + HCl \rightarrow CH_3Cl + HBr$. The fraction of ΔH° originating from $CH_3Br \rightarrow CH_3Cl$ is easily seen to be:

$$\Delta \operatorname{H}^{\circ}(\operatorname{CH}_{3}\operatorname{Br} \to \operatorname{CH}_{3}\operatorname{Cl}) = \Delta \operatorname{E}_{0}^{\circ}(\operatorname{CH}_{3}\operatorname{Br} \to \operatorname{CH}_{3}\operatorname{Cl}) +$$

$$+ \operatorname{RT}\left(\sum_{f=1}^{3n-6} \frac{\frac{\varepsilon_{f}}{kT}}{\operatorname{(CH}_{9}\operatorname{Cl})} - \sum_{f=1}^{\frac{\varepsilon_{f}}{kT}} - \sum_{f=1}^{3n-6} \frac{\frac{\varepsilon_{f}}{kT}}{\operatorname{(CH}_{9}\operatorname{Br})} - \frac{\frac{\varepsilon_{f}}{kT}}{\frac{\varepsilon_{r}}{kT} - 1}\right).$$

For the hydrogen halides tables of $\frac{G^\circ - E_0^\circ}{T}$ are available.¹ Denoting this function by B we can write $G = E_0 + BT$ and

$$H = E_0 + BT + TS.$$

Thus,

$$\Delta \mathrm{H}^{\circ}(\mathrm{HCl} \to \mathrm{HBr}) = \Delta \mathrm{E}^{\circ}_{0}(\mathrm{HCl} \to \mathrm{HBr}) + \mathrm{T} \Delta \mathrm{B}^{\circ}(\mathrm{HCl} \to \mathrm{HBr}) + \\ + \mathrm{T} \Delta \mathrm{S}^{\circ}(\mathrm{HCl} \to \mathrm{HBr})^{2}$$

and

$$\Delta \mathrm{H}^{\circ}(\mathrm{CH}_{3}\mathrm{Br} + \mathrm{HCl} \to \mathrm{CH}_{3}\mathrm{Cl} + \mathrm{HBr}) = \Delta \mathrm{E}_{0}^{\circ}(\mathrm{CH}_{3}\mathrm{Br} + \mathrm{HCl} \to \mathrm{CH}_{3}\mathrm{Br} + \mathrm{HBr})$$

$$+ \operatorname{RT} \left(\sum_{f=1}^{3n-6} \frac{\frac{\varepsilon_{f}}{kT}}{_{CH_{3}Cl} \frac{\varepsilon_{f}}{e^{\frac{\varepsilon_{f}}{kT}} - 1}} - \sum_{f=1}^{3n-6} \frac{\frac{\varepsilon_{f}}{kT}}{_{CH_{3}Br} \frac{\varepsilon_{f}}{e^{\frac{\varepsilon_{f}}{kT}} - 1}} \right) + T\Delta \operatorname{B}^{\circ} (\operatorname{HCl} \to \operatorname{HBr}) + T\Delta \operatorname{S}^{\circ} (\operatorname{HCl} \to \operatorname{HBr}).$$

By insertion of numerical values we get:

| Т°К | T°C | gcal mole ⁻¹ |
|-----|------|-------------------------|
| 0 | -273 | 2500 |
| 298 | 25 | 2450 |
| 606 | 333 | 2340 |

¹ GORDON and BARNES, Journ. Chem. Phys. (1), 692 (1933); GIAUQUE, Journ. Am. Chem. Soc. 54, 1731 (1932).

² Values of S for HCl and HBr in the papers of GORDON and GIAUQUE.

The change in the evolution of heat at a change in temperature of about 300° is of the same order of magnitude as the experimental error.

The evolution of heat at the present reaction can be calculated in advance by using the data available from the literature.¹

 $CH_3Br + HCl \rightarrow CH_3Cl + HBr$ Heat of formation, kcal mole⁻¹ 8.5 22.06 20.1 8.65

Consequently

 $\Delta Q^{\circ} = -\Delta H^{\circ} = (20.1 + 8.65) - (8.5 + 22.06) = -1.81$ kcal.

In this paper it is found that

 $\Delta Q^{\circ} = -2.45$ kcal.

The values of the heat of formation of HCl and HBr undoubtedly are correct, as they are based on consistent thermochemical and spectroscopical data. The data for the heat of formation of CH_3Br and CH_3Cl are mainly due to THOMSEN.² From Thomsen's book and from a paper by BERTHELOT³ it is evident that the determination of the heat of combustion of the methyl halides meets with considerable difficulties. It seems safe to conclude that one or both of Thomsen's values of the heat of formation of CH_3Br and CH_3Cl are incorrect.

IV. Summary.

(1) A relation between the equilibrium constants at two different temperatures of the reaction $CH_3Br + HCl \rightleftharpoons CH_3Cl + HBr$ and spectroscopically determinable quantities has been derived.

¹ Revised and edited by BICHOWSKY and ROSSINI, Thermochemistry of Cheical Substances, New York 1936.

³ THOMSEN, Thermochemische Untersuchungen IV, 86 and 116 (1886). ³ BERTHELOT, Ann. de Chemie et de Physique (V), **23**, 214 (1881).

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(2) An experimental determination of the equilibrium constants at various temperatures was carried through. The reaction wet al. who found $A(CH_3Br) = 87.5 \cdot 10^{-40}$ by direct measurevessel was a 3-l Pyrex bulb. At 606° K k = 0.1352 + 0.0008 was found in the absence of a catalyst. At 357° K k = 0.03433 + 0.00014 was found. At 443° K k = 0.06636 + 0.00100 was found The two last-mentioned determinations were carried through in the presence of an active carbon catalyst.

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(3) The results obtained permit of calculating the greatest moment of inertia of CH₃Br, A (CH₃Br) = $76.5 \cdot 10^{-40}$ gcm² ± 4 per cent. The result is in good agreement with the values found by means of infrared spectroscopy ($82 \cdot 10^{-40} \pm 10$ per cent) and by heat capacity measurements $(78 \cdot 10^{-40} + 8 \text{ per cent})$. At present A (CH₂Br) = $77.5 \cdot 10^{-40}$ gcm² is considered the best value. It is accurate to 4 per cent.

(4) Furthermore, ΔE_0° for the reaction $CH_3Br + HCl =$ $CH_3Cl + HBr$ was found to be 2500 gcal mole⁻¹ \pm 75. The heat of the reaction at various temperatures was calculated. The value found is inconsistent with the value which can be calculated from existing thermochemical data. It is concluded that Thom sen's values for the heat of formation of CH₃Br and CH₃Cl must be incorrect.

The author wants to thank Professor LANGSETH for helpful discussions on the subject.

Note added in proof: In a 'letter' to Phys. Rev. 72, 344, (1947) GORDY, SIMMONS and SMITH have reported the results of micro wave experiments with CH₃Cl and CH₃Br. For CH₃Cl³⁵ A found to be $63.1 \cdot 10^{-40}$ gcm², for CH₃Cl³⁷ A = $64.0 \cdot 10^{-40}$ e. the 'weighed' average for ordinary methyl chloride is 63.4 · 10⁻⁴ A serious discrepancy thus exists between this result and Niel SEN'S value $A = 57.9 \cdot 10^{-40}$ used in this work. The discrepance is hardly explanable by experimental uncertainty. If the micro wave results are confirmed by future experiments the results of the present paper are changed as follows:

pag. 29: A(CH₂Br) = $85.6 \cdot 10^{-40}$ gcm² ± 4 per cent.

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pag. 31: $\Delta E_0^{\circ} = \Delta H_0^{\circ} = 2464 \text{ gcal mol}^{-1} \pm 75$. pag. 32: $\Delta H^{\circ}(298^{\circ} K) = 2414 \text{ gcal mole}^{-1}$. pag. 33: $\Delta Q^{\circ}(298^{\circ} K) = -24.1 \text{ kcal mole}^{-1}$.

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